

Class 10 Mathematics – Chapter: Circles

1. Introduction

A circle is a set of points in a plane that are at a fixed distance (radius) from a fixed point (center).

2. Important Terms

- Center (O): Fixed point in the circle.
- Radius (r): Distance from center to any point on the circle.
- Diameter (d): Distance through the center; $d=2rd = 2rd=2r$.

- Chord: A line segment with endpoints on the circle.
- Arc: A part of the circumference.
- Sector: Region bounded by two radii and an arc.
- Segment: Region bounded by a chord and an arc.

3. Properties of Circles

- Equal chords are equidistant from the center.
- The perpendicular from the center to a chord bisects the chord.

- Diameter is the longest chord.
- Radius is perpendicular to the tangent at the point of contact.

4. Angle Properties

- Angle subtended by a diameter at the circumference is a right angle.
- Angles subtended by the same chord at the circumference are equal.
- Angle in a semicircle is 90° .

5. Equation of a Circle (Cartesian form)

If the center is at (h, k) and radius is r , equation is:

$$(x-h)^2 + (y-k)^2 = r^2$$

For a circle with center at origin $(0, 0)$, it is:

$$x^2 + y^2 = r^2$$

6. Important Formulas

- Circumference = $2\pi r$
- Area = πr^2

7. Important Exam Tips

- Remember key properties and definitions.
- Practice angle property proofs.
- Understand the standard form of circle equations.
- Draw diagrams to visualize problems.